

SC-FDMA Single Carrier FDMA in LTE



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SC-FDMA is a new technology used for uplink in LTE. This white paper explores this technology, its use in LTE and its extension from OFDM.

Introduction

Single Carrier Frequency Division Multiple Access (SC-FDMA) is a promising technique for high data rate uplink communication and has been adopted by 3GPP for it next generation cellular system, called Long-Term Evolution (LTE). SC-FDMA is a modified form of OFDM with similar throughput performance and complexity. This is often viewed as DFT-coded OFDM where time-domain data symbols are transformed to frequency-domain by a discrete Fourier transform (DFT) before going through the standard OFDM modulation. Thus, SC-FDMA inherits all the advantages of OFDM over other well-known techniques such as TDMA and CDMA. The major problem in extending GSM TDMA and wideband CDMA to broadband systems is the increase in complexity with the multipath signal reception. The main advantage of OFDM, as is for SC-FDMA, is its robustness against multipath signal propagation, which makes it suitable for broadband systems. SC-FDMA brings additional benefit of low peak-to-average power ratio (PAPR) compared to OFDM making it suitable for uplink transmission by user-terminals.

3GPP Long Term Evolution

LTE is a next generation mobile system from the 3GPP with a focus on wireless broadband. LTE is based on Orthogonal Frequency Division Multiplexing (OFDM) with cyclic prefix (CP) in the downlink, and on Single-Carrier Frequency Division Multiple Access (SC-FDMA) with cyclic prefix in the uplink. It supports both FDD and TDD duplex modes for transmission on paired and unpaired spectrum.

The generic radio frame has a time duration of 10 ms, consisting of 20 slots of each 0.5 ms. Two adjacent slots form a sub-frame of 1 ms duration, which is also one transmit-time-interval (TTI). Each slot consists of seven OFDM symbols with short/normal cyclic prefix (CP) or six OFDM symbols with long/extended CP.

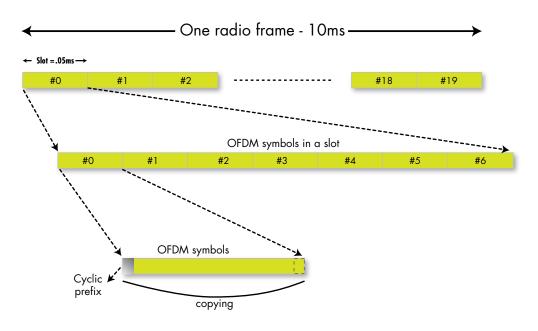


Figure 1. LTE Frame Format

Uplink Transmission

The uplink transmission scheme is based on single-carrier FDMA, more specifically DFTS-OFDM. The uplink sub-carrier spacing $\Delta f = 15$ kHz. There are two cyclic-prefix lengths defined: normal cyclic prefix and extended cyclic prefix corresponding to seven and six SC-FDMA symbols per slot,

$$N_{\text{symb}}^{\text{UL}}$$

respectively. The cyclic prefix timings for uplink are the same as for the downlink.

For short cyclic prefix: $T_{CP} = 160 \times Ts$ for OFDM symbol I = 0

= $144 \times Ts$ for OFDM symbol I = 1, 2, ...6

For long cyclic prefix: T_{CP-} = 512×Ts for OFDM symbol I = 0, 1...5

 $T_{\rm s} = 1/(2048 \times \Delta f)$ is the sampling time for 20 MHz system.



Figure 2. Transmitter scheme of SC-FDMA

The sub-carriers are grouped into sets of 12 consecutive sub-carriers, corresponding to the uplink resource blocks. 12 consecutive sub-carriers in one slot correspond to one uplink resource block – the same as in the downlink – which is depicted in Figure 3. In the frequency domain, the maximum number of resource blocks, N_{RB} , can range from N_{RB-min} = 6 to N_{RB-max} = [110]. Each element in the resource grid is called a resource element and is uniquely defined by the index pair (k,l) in a slot where k and l are the indices in the frequency (subcarrier) and time domain (symbol), respectively.

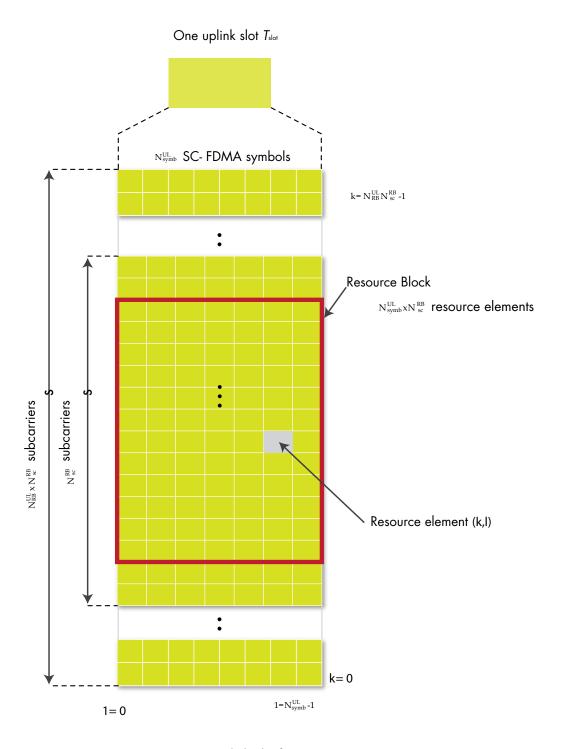


Figure 3. Uplink Slot format

Why OFDM is most favored for broadband systems

Second and third generation mobile systems are based on either TDMA or CDMA technologies. Although these technologies can theoretically be extended to next generation broadband wireless systems, practical implementation issues and complexities limit their acceptance. On the other hand, OFDM offers an easier solution and practical implementation. However, OFDM is not without its issues.

Multipath signal propagation makes the channel response time dispersive; the amount of signal dispersion depends on the environment of operation. For example, the channel dispersion is about 5 micro seconds in typical urban areas and 15 to 20 microseconds in rural and hilly terrain. The factor that affects the receiver is the number of resolvable channel taps over the channel dispersion interval. In a TDMA system, it is the ratio of the channel dispersion to signal symbol time. However, in a CDMA system, it is the number of channel taps with strong energy at chip-time resolution over the channel dispersion period. The channel time dispersion is viewed as the frequency selective or non-selective in the frequency domain. Frequency non-selective channel means the signal over its entire bandwidth will have the same effect due to the multipath channel. This is also called *flat fading*. In the time domain, the channel is not dispersive relative to its symbol time, and hence, there is no ISI. In the *frequency selective channel*, the signal will have independent effects over its bandwidth due to the channel, and it is time dispersive relative to its symbol time.

For narrowband TDMA systems such as GSM, multipath propagation makes the channel frequency non-selective or less selective, making the receiver less complex. Extending TDMA techniques to broadband system makes the receiver complexity unmanageable, as the channel becomes very frequency selective. Let us take a closer look at this problem.

GSM is a 200 kHz channel TDMA system with 270.833 kHz symbol rate with either binary GMSK or 8-PSK modulations. The baseband signal uses partial response signaling, which spreads the symbol to three symbol periods. For a typical urban case with about 5 us channel dispersion, the received signal can have signal dispersion of about 5 symbol periods including its partial response signaling. Hence, a typical GSM receiver requires a 16-state MLSE equalizer for GMSK signal and an 8- or 64-state DFSE equalizer for an 8-PSK EDGE signal. Suppose we want to scale up this technique to a wideband or broadband system by factor of ten, i.e. a 2 MHz system with 2.70833 MHz symbol rate. For the same amount of channel dispersion, the received symbol will be spread over 20 symbol periods. The receiver with an equalizer for 20 channel taps will either be impractical to implement or resort to inferior methods. This problem can easily be dimensioned over a 20 MHz broadband system.

Similarly, WCDMA technique can also be extended to broadband systems, but its complexity increases, as it requires more number of Rake receiver fingers. Complexity, and often the gain of a Rake receiver, are based on the number of Rake fingers the receiver can process. A typical WCDMA Rake receiver requires about 5-8 Rake fingers for a typical urban channel with dispersion of 5 microseconds. More advanced receivers, such as Generalized Rake receivers, require even more fingers as they try to place additional fingers around the desired signal, which are often called interference fingers. Extending WCDMA

to a 20 MHz broadband system will require higher chip rates, meaning that it can resolve channel taps with finer resolution. This results in more fingers for the Rake receiver with strong signal energy. Therefore, extension of WCDMA/HSPA systems to a 20 MHz broadband system requires extension of similar factor on the number of fingers in Rake receiver, and thus its complexity. 3GPP is in the process of defining other ways of extending HSPA system to broadband systems, based on multi-carrier HSPA.

OFDM has become a most favored technique for broadband wireless system due to susceptibility to signal dispersion under multipath conditions. OFDM can also be viewed as a multi-carrier narrowband system where the whole system bandwidth is split into multiple smaller subcarriers with simultaneous transmission. Simultaneous data transmission and reception over these subcarriers are handled almost independently. Each subcarrier is usually narrow enough that multipath channel response is flat over the individual subcarrier frequency range, i.e. frequency non-selective. Another way to look at is that an OFDM symbol time is much larger than the typical channel dispersion. Hence OFDM is inherently susceptible to channel dispersion due to multipath propagation.

One major difference between an OFDM and the TDMA or CDMA techniques is important to note. In traditional systems the symbol detection is on the samples at either symbol or chip rate, and it cares about the carrier-to-interference level only at the sampling points. But, OFDM symbol detection requires that the entire symbol duration be free of interference from its previous symbols, a.k.a. inter-symbol interference. Even though OFDM symbol duration is much larger than channel dispersion, even a small amount of channel dispersion causes some spilling of each OFDM symbol to the next symbol, thus it causes some ISI. However this ISI spill-over is limited to only the initial part of the neighboring symbol. Hence this ISI spill-over at the beginning of each symbol can easily be removed by adding a cyclic prefix to each transmit symbol. Cyclic prefix is the process of extending each symbol by duplicating a portion of the signal at the symbol ends, which is thrown away at the receiver. The amount of symbol extension, i.e. length of cyclic prefixes, is a system design parameter, and it is based on the expected signal dispersion in the environment of system operation. For example, the LTE system uses OFDM symbol of 66 microseconds plus 5 microseconds of cyclic prefix. This means it is susceptible to maximum signal dispersion of 5 microseconds due to multipath channel propagation.

SC-FDMA Modulation

SC-FDMA is a new multiple access technique that utilizes single carrier modulation, DFT-spread orthogonal frequency multiplexing, and frequency domain equalization. It has a similar structure and performance as OFDM. SC-FDMA is currently adopted as the uplink multiple access scheme for 3GPP LTE. Transmitter and receiver structure for SC-FDMA and OFDM are given in Figures 4 and 5. It is evident from the figures that SC-FDMA transceiver has similar structure as a typical OFDM system except the addition of a new DFT block before subcarrier mapping. Hence, SC-FDMA can be considered as an OFDM system with a DFT mapper.

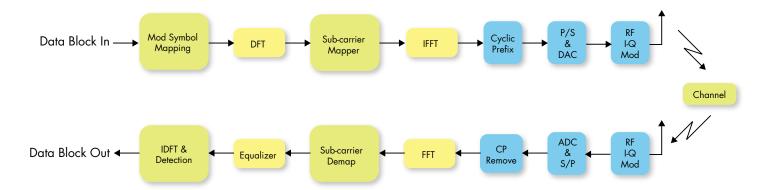


Figure 4. SC-FDMA Transmitter and Receiver

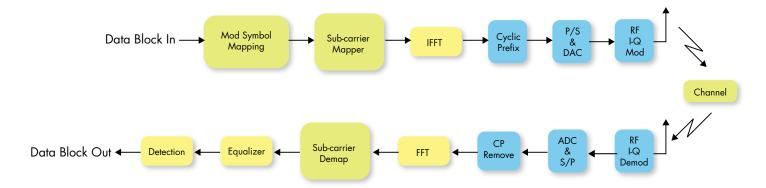


Figure 5. OFDM Transmitter and Receiver

OFDM

As SC-FDMA is built over OFDM modulation, let's first review an OFDM system structure. A typical OFDM transmitter and receiver structure is shown in Figure 2. A transmitter includes a baseband modulator, subcarrier mapping, inverse Fourier transform, cyclic prefix addition, parallel-serial conversion, and a digital-to-analog converter followed by an I-Q RF modulator. Unlike other modulation techniques that operate symbol by symbol, OFDM transmits a block of data symbols simultaneously over one OFDM symbol. An OFDM symbol is the time used to transmit all of subcarriers that are modulated by the block of input data symbols.

The baseband modulator transforms the input binary bits into a set of multi-level complex numbers that corresponds to different modulations formats such as BPSK, QPSK, 16- or 64-QAM.

The type of modulation format used often depends on the signal-to-noise level of the received signal and the receiver ability to decode them correctly. These modulated symbols are then mapped to subcarriers. An inverse-FFT (IFFT) is used to transform the modulated subcarriers in frequency domain to time domain samples.

In general, the same modulation format is used in all the subcarriers to keep the control information overhead small. However, it is possible to have different modulation formats over multiple subcarriers, and it is in fact advantageous in harsh and time varying channel conditions. In a broadband system, the channel is frequency selective over its large system bandwidth, meaning the signal fading on each subcarrier is independent. The interference level on each subcarrier can also be different and vary uniquely with time. It results in a different signal-to-impairment level on each of the subcarriers. Hence, having an appropriate modulation format on these subcarriers would help to maximize the overall system throughput. OFDM system inherits an adaptation of modulation formats to each of the subcarriers depending on channel conditions, and this is called *Channel-dependent scheduling*.

A cyclic prefix block copies a portion of the samples at the end of the time domain samples block (at the IFFT output) to the beginning. Since the DFT/FFT outputs are periodic in theory, copying the samples to the beginning will make the signal continuous. The length of the cyclic prefix depends on the channel delay spread, and is preferably longer than the length of the channel response. At the receiver, the prefix part of the symbol is thrown away as it may contain ISI from its previous symbol. Hence, it removes the effect of ISI caused by the multipath signal propagation. However, the prefix is the overhead in an OFDM system, as it does not carry any useful information.

The block of complex samples are then serialized in the time domain and converted to analog signals. The RF section modulates the I-Q samples to final transmission radio frequency. A corresponding receiver does the inverse operations of the transmitter in the reverse order. A typical OFDM receiver includes an RF section, ADC, parallel-to-serial converter, cyclic prefix remover, Fourier transformer, sub-carrier demapper, equalizer and detector.

OFDM to SC-FDMA

The main difference between OFDM and SC-FDMA transmitter is the DFT mapper. After mapping data bits into modulation symbols, the transmitter groups the modulation symbols into a block of N symbols. An N-point DFT transforms these symbols in time domain into frequency domain. The frequency domain samples are then mapped to a subset of M subcarriers where M is typically greater than N. Similar to OFDM, an M-point IFFT is used to generate the time-domain samples of these subcarriers, which is followed by cyclic prefix, parallel to serial converter, DAC and RF subsystems.

Frequency Spread OFDM

Each data symbol is DFT transformed before mapping to subcarriers, hence the SC-FDMA is called *DFT-precoded* OFDM. In a standard OFDM, each data symbol is carried on a separate subcarrier. In SC-FDMA, multiple subcarriers carry each data symbol due to mapping of the symbols' frequency domain samples to subcarriers. As each data symbol is spread over multiple subcarriers, SC-FDMA offers spreading gain or frequency diversity gain in a frequency selective channel. Thus, SC-FDMA can be viewed as *frequency-spread OFDM* or *DFT-spread OFDM*.

Subcarrier Mapping

DFT output of the data symbols is mapped to a subset of subcarriers, a process called subcarrier mapping. The subcarrier mapping assigns DFT output complex values as the amplitudes of some of the selected subcarriers. Subcarrier mapping can be classified into two types: localized mapping and distributed mapping. In localized mapping, the DFT outputs are mapped to a subset of consecutive sub-carriers thereby confining them to only a fraction of the system bandwidth. In distributed mapping, the DFT outputs of the input data are assigned to subcarriers over the entire bandwidth non-continuously, resulting in zero amplitude for the remaining subcarriers. A special case of distributed SC-FDMA is called interleaved SC-FDMA, where the occupied subcarriers are equally spaced over the entire bandwidth. Figure 6 is a general picture of localized and distributed mapping.

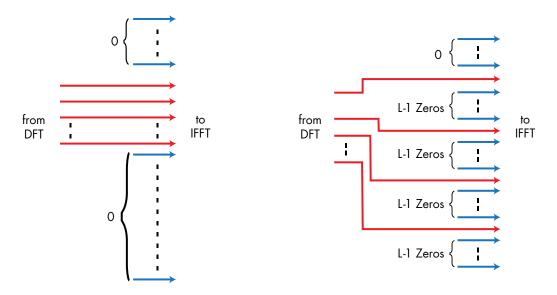


Figure 6. Localized mapping vs. Distributed mapping

An example of subcarrier mapping is shown in Figure 7. This example assumes three users sharing 12 subcarriers. Each user has a block of four data symbols to transmit at a time. The DFT output of the data block has four complex frequency domain samples, which are mapped over 12 subcarriers using different mapping schemes.

SC-FDMA inherently offers frequency diversity gain over the standard OFDM, as all information data is spread over multiple subcarriers by the DFT mapper. However, the distributed SC-FDMA is more robust with respect to frequency selective fading and offers additional frequency diversity gain, since the information is spread across the entire system bandwidth. Localized SC-FDMA in combination with channel-dependant scheduling can potentially offer multi-user diversity in frequency selective channel conditions.

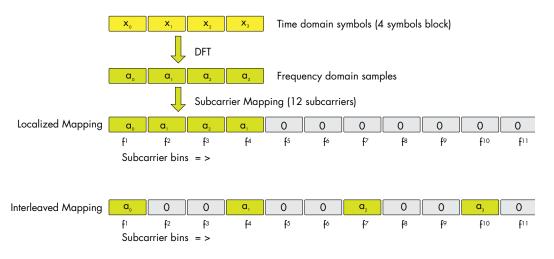


Figure 7. Subcarrier Mapping Example

Single Carrier Modulation

Based on SC-FDMA's structure, the reasons for some of its names, such as DFT-precoded OFDM or DFT-spread OFDM, are clear. But for the use of 'Single Carrier' in its name, SC-FDMA, is not as obvious and is often the reason why is not explained,. Unlike the standard OFDM where the each data symbol is carried by the individual subcarriers, the SC-FDMA transmitter carries data symbols over a group of subcarriers transmitted simultaneously. In other words, the group of subcarriers that carry each data symbol can be viewed as one frequency band carrying data sequentially in a standard FDMA. For some of the subcarrier mappings, the time domain representation of the IFFT output, as shown in Figures 8 and 9, will give more insight on the SC-FDMA signal. It can be mathematically shown that the SC-FDMA baseband time domain samples after IDFT or IFFT is the original data symbol set repeated in time domain over the symbol period.

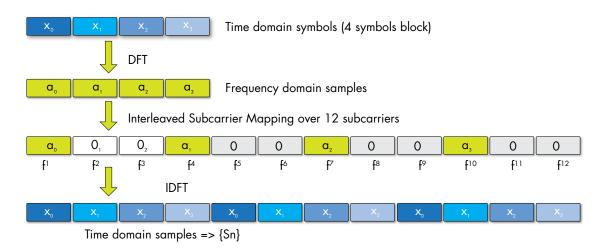


Figure 8. Time domain representation of Interleaved SC-FDMA

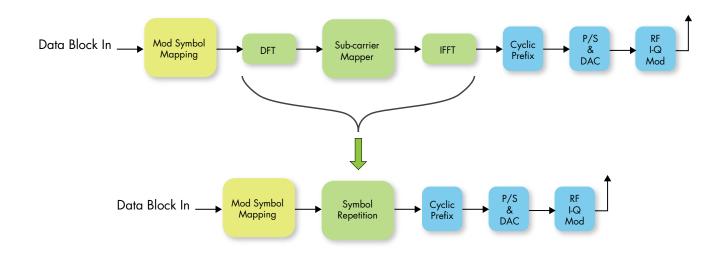


Figure 9. Simplified Interleaved SC-FDMA Transmitter

PAPR analysis

SC-FDMA offers similar performance and complexity as OFDM. However, the main advantage of SC-FDMA is the low PAPR (peak-average-power ratio) of the transmit signal. PAPR is defined as the ratio of the peak power to average power of the transmit signal. As PAPR is a major concern at the user terminals, low PAPR makes the SC-FDMA the preferred technology for the uplink transmission. PAPR relates to the power amplifier efficiency at the transmitter, and the maximum power efficiency is achieved when the amplifier operates at the saturation point. Lower PAPR allows operation of the power amplifier close to saturation resulting in higher efficiency. With higher PAPR signal, the power amplifier operating point has to be backed off to lower the signal distortion, and thereby lowering amplifier efficiency. As SC-FDMA modulated signal can be viewed as a single carrier signal, a pulse shaping filter can be applied to transmit signal to further improve PAPR.

PAPR comparison between OFDM and SC-FDMA variations such as interleaved SC-FDMA and localized SC-FDMA has been done in [2]. With no pulse shaping filters, interleaved-SC-FDMA shows the best PAPR. Compared to OFDM PAPR, the PAPR of interleaved SC-FDMA with QPSK is about 10 dB lower, whereas that of localized SC-FDMA is only about 3 dB lower. With 16-QAM, these levels are about 7 dB and 2 dB lower respectively. Therefore, interleaved SC-FDMA is a preferred modulation technique for lower PAPR. Pulse shape filtering of SC-FDMA in fact degrades the PAPR level of interleaved SC-FDMA whereas it shows no effect with localized SC-FDMA.

References

- [1] Jens Berkmann, et al., "On 3G LTE Terminal Implementation Standard, Algorithms, Complexities and Challenges", IWCMC 2008 Mobile Computing Symposium, 2008
- [2] Hyung G. Myung, Junsung Lim, and David J. Goodman, "Single Carrier FDMA for Uplink Wireless Transmission." IEEE Vehicular Technology, Sept 2006
- [3] 3GPP TR 25.912 v 7.1.0, "Feasibility study for evolved Universal Terrestrial Radio Access (UTRA) and Universal Terrestrail Radio Access Network (UTRAN)," Release 7
- [4] 3GPP TS 36.300 v8.7.0, "Evolved Universal Terrestrial Radio Access (E-UTRA) and Evolved Universal Terrestrial Radio Access Network (E-UTRAN); Overall description; Stage 2," Release 8
- [5] 3GPP TS 36.211 v8.4.0, "Evolved Universal Terrestrial Radio Access (E-UTRA); Physical Channels and Modulation," Release 8
- [6] 3GPP TS 36.212 v8.4.0, "Evolved Universal Terrestrial Radio Access (E-UTRA); Multiplexing and Channel coding," Release 8
- [7] 3GPP TS 36.213 v8.4.0, "Evolved Universal Terrestrial Radio Access (E-UTRA); Physical layer procedures," Release 8



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